The Penryn Partnership Mathematics Calculation Policy 2017







Progression in Calculations

Addition

	2		
Objective and	Concrete	Pictorial	Abstract
Strategies			
STEP ONE Combining two parts to make a whole: part- whole model	<image/>	Image: state s	5 4 + 3 = 7 10= 6 + 4 Use the part-part whole diagram as shown above to move into the abstract.
STEP TWO		12 + 5 = 17	5 + 12 = 17
Starting at the bigger number and counting on	Start with the larger number on the bead string and then count on to the smaller number 1 by 1 to find the answer.	Start at the larger number on the number line and count on in ones or in one jump to find the answer.	Place the larger number your head and count on the smaller number to fir your answer.

STEP THREE Regrouping to make 10.	6 + 5 = 11	3+9=	Use pictures or a number line. Regroup or partition the smaller number to make 10.	7 + 4= 11 If I am at seven, how many more do I need to make 10. How many more do I add on now?
	Start with the bigger number and use the smaller number to make 10.	9 + 5 = 14 + 1 + 4	13 (14) 15 16 17 18 19 20	
STEP FOUR Adding three single digits	4 + 7 + 6= 17 Put 4 and 6 together to make 10. Add on 7.		+ + + + + + + + + + + + + + + + + + +	4 + 7 + 6 = 10 + 7 $= 17$ Combine the two numbers that make 10 and then add on the remainder.
	Following on from making 10, make 10 with 2 of the digits (if possible) then add on the third digit.	Add together three groups of picture to recombine the group	-	

STEP FIVE	24 + 15= Add together the ones tens. Use the Base 10 moving onto place value	blocks first before		e base 10 blocks and place value raw the counters to help them to	$\frac{Calculations}{21 + 42} =$	
Column method- no			T	0	21 + 42 -	
regrouping					21	
					+ <u>42</u>	
		•				



. 1 4

Subtraction

Objective and	Concrete	Pictorial	Abstract
Strategies			
STEP ONE	Use physical objects, counters, cubes etc to show how objects can be taken	Cross out drawn objects to show what has been taken away.	18 -3= 15
Taking away ones	away.		8 – 2 = 6
		△△△ △△△ 15-3=12	
	6-2=4		
STEP TWO	Make the larger number in your subtraction. Move the beads along your bead string as you count backwards in	Count back on a number line or number track	Put 13 in your head, count back 4. What number are you at? Use your fingers to
Counting back	ones.	9 10 11 12 13 14 15	help.
	13 – 4	Start at the bigger number and count back the smaller number showing the jumps on the number line.	
	Use counters and move them away from the group as you take them away counting backwards as you go.	-10 -10	
		-1 -1 -1 34 35 36 37 47 57	
		This can progress all the way to counting back using two 2 digit numbers.	



STEP FIVE	14 - 9 =		400
		$13 - 7 = 6$ _4 _3	16 – 8=
Make 10		0 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20	How many do we take off to reach the next 10?
	Make 14 on the ten frame. Take away	Start at 13. Take away 3 to reach 10. Then take away the remaining 4 so you have taken away 7 altogether. You	How many do we have left to
	the four first to make 10 and then	have reached your answer.	take off?
	takeaway one more so you have taken away 5. You are left with the answer of		
	9.		







Multiplication

Objective and Strategies	Concrete	Pictorial	Abstract
STEP ONE Doubling	Use practical activities to show how to $ \begin{array}{c} $	Draw pictures to show how to double a number. Double 4 is 8	$\begin{array}{c} 16 \\ 10 \\ 10 \\ 10 \\ 10 \\ 10 \\ 10 \\ 10 \\$
STEP TWO Counting in multiples	Count in multiples supported by concrete objects in equal groups.	Use a number line or pictures to continue support in counting in multiples.	Count in multiples of a number aloud. Write sequences with multiples of numbers. 2, 4, 6, 8, 10 5, 10, 15, 20, 25, 30

STEP THREE Repeated addition	3 + 3 + 3 Use different objects to add equal groups.	There are 3 plates. Each plate has 2 star biscuits on. How many biscuits are there? There are 3 plates. Each plate has 2 star biscuits on. How many biscuits are there? 2 add 2 add 2 equals 6 5 5 5 5 5 5 5 5	Write addition sentences to describe objects and pictures. 2+2+2+2+2=10
STEP FOUR Arrays- showing commutative multiplication	Create arrays using counters/ cubes to show multiplication sentences.	Draw arrays in different rotations to find commutative multiplication sentences.	Use an array to write multiplication sentences and reinforce repeated addition. 00000 5+5+5=15 3+3+3+3+3=15 $5 \times 3 = 15$ $3 \times 5 = 15$

STEP FIVE

Grid Method



Show the link with arrays to first

Move on to using Base 10 to move towards a more compact method.



Move on to place value counters to show how we are finding groups of a number.We are multiplying by 4 so we need 4 rows.



Children can represent the work they have done with place value counters in a way that they understand.

They can draw the counters, using colours to show different amounts or just use circles in the different columns to show their thinking as shown below.



Start with multiplying by one digit numbers and showing the clear addition alongside the grid.

×	30	5
7	210	35

210 + 35 = 245

Moving forward, multiply by a 2 digit number showing the different rows within the grid method.

1	10					8	
10		1	00			80	
3		3	30			24	
						-	
Х		1000	300	40		2	
10	ł	10000	3000	400	D	20	
8		8000 2400)	16	

STEP SIX Column multiplication	Children can continue to be supported by place value counters at the stage of multiplication.	Bar modelling and n when solving proble formal written method $\boxed{51 59 68} = 8 \times 60 = 480 \\ 480 - 8 = 472$	ms with multiplica ods.		Start with long multiplication, reminding the children about lining up their numbers clearly in columns. If it helps, children can write out what they are solving next to their answer. $x \frac{32}{x \cdot 24} = (4 \times 2)$ $120 (4 \times 30)$ $40 (20 \times 2)$ $600 (20 \times 30)$ $7 4$ $\frac{x 6 3}{1 2}$ $2 1 0$ $2 4 0$ $\frac{x 6 3}{1 2}$ $2 1 0$ $2 4 0$ $\frac{x 6 3}{4 6 6 2}$ This moves to the more compact method.
		5172 <u>x 38</u> 41376 + <u>155160</u> <u>196536</u>	2 151 5172 <u>x 38</u> 41376 + <u>155160</u> <u>196536</u> 1	$5172 \\ x 38 \\ 41376 \\ 151 \\ + 155160 \\ 2 \\ 196536 \\ 1$	2 3 1 1 3 4 2 X 1 8 1 3 4 2 0 OR 1 3 4 2 0 1 0 7 3 6 2 4 1 5 6 1 1 5 6

Division

Objective and	Concrete	Pictorial	Abstract
Strategies			
STEP ONE Sharing objects into		Children use pictures or shapes to share quantities.	Share 9 buns between three people. $9 \div 3 = 3$
groups	I have 10 cubes, can you share them equally in 2 groups?	$3 \div 2 = 4$	
STEP TWO Division as grouping	Divide quantities into equal groups. Use cubes, counters, objects or place value counters to aid understanding.	Use a number line to show jumps in groups. The number of jumps equals the number of groups. 0 1 2 3 4 5 6 7 8 9 10 11 12 3 3 3 3 3 3	28 ÷ 7 = 4 Divide 28 into 7 groups. How many are in each group?
	••••• •••••• ••••• ••••• <t< td=""><td>Think of the bar as a whole. Split it into the number of groups you are dividing by and work out how many would be within each group.</td><td></td></t<>	Think of the bar as a whole. Split it into the number of groups you are dividing by and work out how many would be within each group.	
	96 ÷ 3 = 32	20	
	······································	20 ÷ 5 = ? 5 x ? = 20	

STEP THREE Division within arrays	Link division to multiplication by creating an array and thinking about the number sentences that can be created.	Image: Second
STEP FOUR	Eg $15 \div 3 = 5$ $5 \times 3 = 15$ $15 \div 5 = 3$ $3 \times 5 = 15$ $14 \div 3 =$ Divide objects between groups and	Draw an array and use lines to split the array into groups to make multiplication and division sentences.Complete written divisions and show the remainderJump forward in equal jumps on a number line then see how many more you need to jump to find a remainder.Complete written divisions and show the remainder
Division with a remainder	see how much is left over	Using r. Using r. $29 \div 8 = 3$ REMAINDER 5 $\uparrow \uparrow \uparrow \uparrow$ $\uparrow \uparrow \uparrow \uparrow$ $\downarrow \lor \downarrow \uparrow$ $\downarrow \lor \downarrow$ $\downarrow \lor \lor$ $\downarrow \lor \downarrow$ $\downarrow \lor$ $\downarrow \lor$ \downarrow $\downarrow \lor$ \downarrow \downarrow \downarrow \downarrow \downarrow \downarrow \downarrow \downarrow



•		Dividing by 2 digit numbers					
		15	7	4 ⁷ 3	9 ¹³ 5		
0		By listing the 15 times table by repeated addition					
r.		15,30,45,60,75,90,105, 120,135,					
		OR					
			1 7	4	7 ³ 5		
		5	7	² 3	³ 5		
		2	4	4 1 4	9 2 7		
		3	1	.4	-7		
	By dividing by factors of the number.						
		<u>NOTE</u>					
		This will not work					
		for prime					
		numbers					

6 r 2

8 6 $r\frac{2}{5}$

32

³2

8

⁴3

⁴3

